

Estimating Intra-Household Bargaining Power When Outside Options Are Endogenous

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Abstract: We generalize the collective model of the family to let partners choose their outside options, whether to act on them, and how to allocate shared resources. To do so, we apply Harsanyi's (1986) generic games framework to a limited-commitment collective model where a family's real consumption opportunities depend on each partners' specified outside option. We demonstrate uniqueness and existence of the solution by applying Rubinstein, Safra, and Thomson's (1992) appeals-immunity solution concept. We demonstrate that the expected value of bargaining power is semi-parametrically identified in an ordinal framework; the research need not assume specific utility or social welfare functional forms. In addition to empirical tractability and analytical precision, this update to the collective model provides a more nuanced view of intra-household bargaining power: partner's with a greater capacity to specify more damaging threats will have more control over the decision-making process, regardless of whether they act on those threats. (JEL: D1, D6, D7)

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1 Introduction

Economists have used the collective model of the family (Chiappori 1988, 1992; Apps and Rees, 1988) to empirically study power dynamics in the family for the last three decades (Donni and Molina, 2018). A key explanation for why certain power dynamics obtain in equilibrium is that partners' next best alternative to the collective allocation — their "outside options" — are more or less valuable (Mazzocco, 2007; Ligon, 2011). The partner with a more valuable outside option has more bargaining power in the family.

However, the collective model has two critical shortcomings that limit economists' ability to measure power dynamics. First, researchers must make strong assumptions about the nature of each partners' outside options. The standard approach is to assume the outside option is divorce, or some nebulous inefficient allocation within the family (Chiappori and Mazzocco, 2017). Assuming that each person's outside option takes the same form introduces misspecification error, and threatens identification. Letting each person endogenously choose their outside option in a generic game framework (Harsanyi, 1986) fixes this problem. Second, researchers must make strong functional form assumptions for social welfare, utility, production, and consumption functions, further introducing the possibility of misspecification error. Proceeding from an ordinal framework instead of a cardinal framework solves this problem.

In this paper, we address these two shortcomings of the collective model. We generalize the collective model with limited-commitment to a generic games framework, and we demonstrate semi-parametric identification of the sharing rule in an ordinal setting. To show that the solution is unique, we use the appeals-immune solution concept developed by Rubinstein, Safra, and Thomson (1992) and advanced by Hanany and Safra (2000). We suggest two estimation strategies: one that does not require economists to specify functional forms for utility, social welfare, production, and consumption functions; and one that does.

To consider how these advancements contribute to economists' ability to measure bargaining power in the family, consider two recent, innovative papers on domestic abuse and power in the family — Ramos (2016), who studies data from northern Ecuador in 2011, and Lewbel and Pendakur (2019) who study data from Bangladesh in 2015. In both papers, men are allowed to choose some level of violence in the family (though only Ramos [2016] recovers a demand function for violence). The benefit of violence is that men gain control over the decision-making process — their "resource share" increases. The cost is that women are harmed, which is a negative outcome in itself, of course, and can also reduce productive possibilities for the household. By choosing to be violent with some positive frequency, men consume a larger portion

of a smaller amount of surplus, and more overall than if they had not been violent. These papers advance our ability to measure power dynamics in inefficient families.¹

However, both papers are subject to the limitations of the collective model already discussed. Ramos (2016) assumes that only men can specify and act on threats. In fact, women may be able to take some recourse to violence, like moving in with their parents temporarily, allocating labor or assets in a socially-inefficient way, or filing for a divorce. By assuming that women have no outside option, Ramos (2016) may overestimate the benefits that accrue to men from violence. Further, her work may be subject to misspecification error in the functional forms for utility and production functions, and the elasticity of women's labor allocations to violence.

Lewbel and Pendalur (2019) incorporate violence into the collective model developed by Browning, Chiappori, and Lewbel (2013) and use the identification strategy developed in Dunbar, Lewbel, and Pendakur (2013). Violence shifts the family from an efficient consumption technology to an inferior one (imposes higher shadow prices for the family). However, they are unable to derive a demand function for violence, which limits the predictive capacity of their model. Furthermore, they only demonstrate identification when threats take a binary value (either the husband abused his wife or he didn't). They are unable to study how more damaging threats might impact power dynamics, or explain why certain levels of violence obtain in equilibrium. They are unable to assess what effect the possibility of women filing for divorce might have on power dynamics.

The generalization of the collective model we develop in this paper solves these problems. In our generic game, we let both individuals in a couple choose their outside option (or "threat" in Harsanyi's language) from a large set that includes divorce, physical and emotional violence, damage to productive assets or the consumption technology, or some combination of these. We relate these threats to each other by quantifying their impact on the real shadow income that each person has at their disposal in the collective setting (or individually if they divorce), which is similar to the approach in Lewbel and Pendakur (2019). If implemented, more damaging threats reduce the total surplus available to the family more (move the Pareto frontier inward). Regardless of implementation, more damaging threats grant the partner who made them more control over the decision making process (moving the

¹Similar arguments about the individual rationality of socially-inefficient behavior could be applied to explain a broad range of observed behaviors. Udry (1996) documents intra-household inefficiencies in the allocation of fertilizer across men's and women's agricultural plots using data from 1981-1985 in Burkina Faso. Reallocating some fertilizer from men's plots to women's would increase household income by 6% on average. de Mel, McKenzie, and Woodruff (2009) find evidence of inefficient demand for productive assets more broadly in experimental data from Sri Lanka, and Schaner (2015) documents that families in Kenya engage in inefficient savings behavior when partners discount future consumption at different rates. Walther (2018) documents partners choosing inefficient labor allocations in Malawi in order to gain more control over the decision-making process. See Basu (2006) for a theoretical treatment of the topic.

collective outcome along the Pareto frontier).

Our model provides analytical clarity on the role of threats in determining the quantity and division of surplus within the family. Power, it becomes clear, is an individual's capacity to specify a more damaging threat in order to gain additional control over the family decision-making process. The family's sharing rule is determined by power dynamics within the family. Also, unlike the models in the two example papers, power in our framework is influenced by the threats that partners specify, regardless of whether they act on them. Families where men might be violent, but are not, will have different power dynamics from families where men do not have an inclination towards violence. The two models we've discussed, and other collective models, are unable to make this distinction. So Harsanyi's generic games framework adds nuance to the collective model's capacity to analyze power dynamics within families, as well as adding empirical tractability.

We also introduce two semi-parametric identification strategies that enable researchers to bring this model to data, and describe the corresponding data requirements for each. One of these strategies is ordinal (does not require cardinal assumptions on utility functions or the social welfare function) and one is cardinal. In the ordinal approach, researchers assume that preferences are jointly distributed across families in the population in some way. This distribution assumption implies a functional form for the expected value of the sharing rule in the family, which can be recovered from panel data with information on threats and violence, demographic characteristics, partners' earnings profiles, and at least two waves of information. In the cardinal approach, researchers can pursue a more conventional strategy of assuming a social welfare function, utility functions, a functional form for the family's production and consumption technologies, and a functional form for the sharing rule, and so recover the family's decision-making structure. This model can be estimated using cross-sectional data with information on threats and violence, earnings profiles, household demand, and demographic information. In both approaches, researchers can instrument for violence in order to correct for measurement error.

2 A Model of Household Decision Making with Limited Commitment and Endogenous Threat Points

Consider two married partners, indexed f and m , who bargain over consumption and production decisions, who may choose to be non-cooperative to some degree, and who can end the partnership via divorce. The choices that the individuals make will depend on their preferences, the bargaining power each partner has, prices, and income. The choices they make can shape the lives of their dependants. We

build a model with these features and derive the households' demand functions for consumption goods, derive individuals' demand functions for violence and other forms of non-cooperation, predict whether divorce will occur, and show how the distribution of surplus within the family is related to the threat and use of violence, and how well-off partners are in the case of divorce.

Following the definitions introduced by Rubinstein, Safra, and Thomson (1992), let a *bargaining problem* be a triple $\langle \theta, \succsim_f, \succsim_m \rangle \in (\Sigma_f \times \Sigma_m) \times \rho^2$, where θ is a bargaining outcome defined over the set of possible outcomes $\Sigma_f \times \Sigma_m$; and \succsim_f and \succsim_m are partners' preferences over states of the world induced by their bargaining outcomes, which are elements of the set of permissible preferences, ρ .² The permissible actions are threats of non-cooperation that each partner specifies but does not necessarily need to act on. They include physical or emotional violence, divorce, and milder punishments like neglecting agreed-upon duties or chores.

A *solution* to the *bargaining problem* is a pair of threats and indicators for whether individuals act on them, $\theta^* = (\theta_f^*, \theta_m^*, I_f^*, I_M^*) \in (\Sigma_f^* \times \Sigma_m^*)^* \times \{0, 1\}^2$, where $(\Sigma_f^* \times \Sigma_m^*)^* \subset (\Sigma_f \times \Sigma_m)$ is the set of possible actions that are *individually rational*. After defining this term, and *appeals immunity*, we follow Hanany and Safra (2000) to show that a unique solution exists to this bargaining problem.

The concept of *appeals immunity* is introduced in Rubinstein, Safra, and Thomson (1992) for preferences defined over lotteries. We introduce the analog for preferences defined over consumption bundles without uncertainty. The intuition of *appeals immunity* has to do with the willingness to pay of both partners to change from one specified pair of (*individually rational* and permissible) threats to another such pair. A pair will be successfully appealed if there exists a transfer from one partner to another that makes both partners willing to shift to the specified alternative. The unique *appeals-immune* pair of threats is given by the Nash product of functions that relate the partners' preferences over an alternative and a reference outcome to their willingness to pay to switch from the reference to the alternative. Rubinstein, Safra, and Thomson (1992) call such functions "induced utility functions" and Hanany and Safra (2000) generalize their usage to a broad set of permissible preferences. While derivatives are not defined over the set of preferences, the induced utility functions are differentiable.

We develop the concept of *individual rationality* by applying Harsanyi's (1986) generic games framework to a specific type of household model: a collective model with limited commitment (as discussed by discussed by Mazzocco [2007] and Ligon [2011]) and with a generic consumption technology (as in Browning, Chiappori, and

²We will define the set of permissible preferences more explicitly after introducing two key more concepts developed by Rubinstein, Safra, and Thomson (1992) and advanced by Hanany and Safra (2000): induced utility functions, and appeals-immune solutions.

Lewbel [2013]). We augment this model with a production function to expand the space of threats available to partners to include threats such as "I won't share my fertilizer with you for your crops." We know such inefficiencies exist (e.g. Udry, 1996) and incorporating them into a model of power and threats rationalizes this type of potential inefficiency in household production. Following Lewbel and Pendakur (2019), we specify the consumption and production technologies as functions of the threats and the dummy variables for whether partners act on them. While the concept of *appeals-immunity* is independent of the bargaining structure we specify, the concept of *individual rationality* depends on the structure of the household bargaining process. In short, an *individually-rational* threat is one that maximizes an individual's utility in the resulting collective optimization problem.

The specified structure for our *bargaining problem* is a limited-commitment collective model nested within Harsanyi's generic game. As such, partners first choose optimal threats in a non-cooperative bargaining game. Then, they use these threats to play a limited-commitment cooperative bargaining game with a (conditionally) Pareto efficient outcome. This nested game allows the econometrician to recover the sharing rule as a function of the specified threats, the household demand functions, and via the participation constraints, decision rules for whether either player acts on their specified threat. Applying the idea of *appeals-immunity* lets us specify the unique, *individually-rational* permissible pair of threats that solves the *bargaining problem*.

By applying this very general structure to this *bargaining problem*, we can show that each *solution* is related to a specific set of household demand functions and the households' sharing rule. As such, with this specific bargaining structure, a *solution* can be written as the superset $(\theta^*, \eta^*, z^*(p, y), x_f^*(p, \eta^*y), x_m^*(p, (1 - \eta^*)y), l_f^*, l_m^*) \in (\Sigma_f^* \times \Sigma_m^*)^* \times \{0, 1\}^2 \times [0, 1] \times (\mathbb{R}_+^n)^3 \times [0, 24]^2$, where the sharing rule between the two partners takes some value between zero and one, the household demand and individuals' consumption equivalent functions are n -vectors of weakly positive numbers, and labor allocations are bounded between zero and twenty-four hours of work per day.

Intuition for the concept of *individual rationality* emerges from this bargaining structure and the corresponding solution set. When partners specify a more damaging threat, they get an increased resource share. However, if they carry out the threat, the total surplus available to the family is reduced. This is captured by a reduction in the quality of the consumption and production technologies. A threat is *individually rational* if it equates the marginal benefit (increased control over the collective decision making process) to the marginal cost (potential reduction in the value of the production and consumption technologies, reducing the amount of total household surplus). There may be multiple permissible and *individually-rational*

pairs of threats, but only one of them is *appeals-immune*.

One of the most damaging threats available to each player is divorce, which forces the partners to abandon their shared consumption and production technologies for private technologies. For instance, if partners cease cohabitation after divorce, then they won't be able to split housing or utility bills, but will have separate bills to pay for housing, heating, and water usage. They lose the ability to benefit from specialization within the household, and from positive externalities that accumulate from consuming locally-public goods.

2.1 Formally Defining Appeals Immunity

A key element of our argument is that each set $(\theta_f^*, \theta_m^*, I_f^*, I_m^*)$ has a corresponding unique set of consumption and labor allocations for each partner $(x_f^*, x_m^*, l_f^*, l_m^*)$. We define preferences over these consumption bundles. The bijection is critical because it translates partners' preference relations over consumption bundles to preference relations over threats in an order-preserving way. We show that this bijective relationship holds in the next section, and proceed as if it were true to define appeals-immune outcomes here.

Let $\Delta_i : (\Sigma_f \times \Sigma_m) \times \{0, 1\}^2 \rightarrow R^n$ be the bijective function relating possible *bargaining solutions* to the corresponding bundle that each individual consumes. Then, for two possible bargaining solutions θ^{*a} and θ^{*b} and their corresponding consumption outcomes x_i^{*a} and $x_i^{*b} \forall i \in \{f, m\}$, $x_i^{*a} \succ_i x_i^{*b} \implies \Delta(\theta^{*a}) \succ_i \Delta(\theta^{*b}) \implies \theta^{*a} \succ_i \theta^{*b}$ and $x_i^{*a} \succsim_i x_i^{*b} \implies \Delta(\theta^{*a}) \succsim_i \Delta(\theta^{*b}) \implies \theta^{*a} \succsim_i \theta^{*b}$. This allows us to search for an optimal threat over partners' preferences spaces (and the spaces of permissible threats) directly, as opposed to continually referencing the corresponding consumption bundle for each partner. As it turns out, the bijective Δ_i is a differential operator that satisfies the first order conditions from the nested game.

Consider induced utility functions, which map from the *solution* space to the real numbers, and describe a person's willingness to pay to transition from a reference *solution* to an alternative. Let $u(\succsim_i, \theta^r, \theta)$ be such a function for $i \in \{f, m\}$, where θ^r is a reference solution and θ is a specified alternative, $u : \rho \times ((\Sigma_f^* \times \Sigma_m^*)^* \times \{0, 1\}^2)^2 \rightarrow \mathbb{R}$. Because both outcomes, θ^r and θ , are associated with specific private equivalent consumption bundles for each person, and because people have preferences over these consumption bundles, partners indirectly have preference relations over θ^r and θ . People always prefer the outcome where their partner does not carry out the threat to the outcome where their partner chooses to carry out their threat. Note that $u(\succsim_i, \theta^r, \theta)$ is differentiable.³

³Formally, for some $\alpha \in [0, 1]$, $u(\succsim_i, \alpha\theta^r + (1 - \alpha)\theta, \theta) = \alpha u(\succsim_i, \theta^r, \theta)$. Convex mixtures of the reference and alternatives result in averages over willingness to pay amounts in a smooth manner. When the reference threat changes by a small amount, the willingness to pay changes by a small

The value $u(\succsim_i, \theta^r, \theta)$ is a compensating variation value. It makes that partner indifferent between two pairs of threats by changing the value of the consumption bundles the right amount. For partner f , this value solves: $x_f(p, \eta^{*r}y + u(\succsim_f, \theta^r, \theta)) \sim_f x_f(p, \eta^*y)$. Similarly, for partner m , this compensating variation amount is the one that makes them indifferent between the consumption bundle associated with the reference bargaining solution, and the alternative: $x_m(p, (1 - \eta^{*r})y + u(\succsim_m, \theta^r, \theta)) \sim_m x_m(p, (1 - \eta^*)y)$. When $\theta^r \succ_i \theta \forall i \in \{f, m\}$, $u(\succsim_i, \theta^r, \theta) > 0$, when $\theta \succ_i \theta^r$, $u(\succsim_i, \theta^r, \theta) < 0$, and when $\theta^r \sim_i \theta$, $u(\succsim_i, \theta^r, \theta) = 0$. Note that if $\theta^r \succ_i \theta$, then $u(\succsim_i, \theta, \theta^r) < 0$. These values help us define the concept of appeals-immunity in a context where preferences are defined over consumption bundles, not lotteries (i.e. there is no probability space in our *bargaining problem* or *solution*).

Definition 1: Let $\langle \theta, \succsim_f, \succsim_m \rangle \in (\Sigma_f \times \Sigma_m) \times \rho^2$, be a bargaining problem. Let $\theta, \theta^r \in (\Sigma_f \times \Sigma_m) \times \{0, 1\}^2$ be two potential solutions to $\langle \theta, \succsim_f, \succsim_m \rangle$. The reference outcome θ^r is immune to the appeal of the alternative θ in $\langle \theta, \succsim_f, \succsim_m \rangle$ if one of the following is true:

1. $\theta^{*r} \succ_f \theta^*$ and $x_f(p, \eta^{*r}y) \succ_f x_f(p, \eta^*y + \tau_m)$ where $\tau_m \in [0, u(\succsim_m, \theta^r, \theta)]$, or
2. $\theta^{*r} \succ_m \theta^*$ and $x_m(p, (1 - \eta^{*r})y) \succ_m x_m(p, (1 - \eta^*)y + \tau_f)$ where $\tau_f \in [0, u(\succsim_f, \theta^r, \theta)]$

This definition simply says that there is no transfer that one partner could give to the other that makes both happy to switch from the reference threats to an alternative potential solution. In the first condition, partner m wants to switch and can offer some transfer amount to partner f equal to or less than their compensating variation value, but this is not enough to induce partner f to switch. In the second condition, the opposite scenario plays out. Partner f wants to switch but partner m does not, and there is not a feasible transfer from f to m that makes m prefer to switch. In these cases, the reference outcome will remain the family's outcome despite the appeal to switch to an alternative.

Consider an example based on Ramos' (2016) work on violence and power in the household. In her study context, northern Ecuador in 2011, 35% of married men abuse their partners and only a small fraction of those relationships end in divorce. In this context, men's threat would be some form of physical, sexual, or emotional abuse (or some combination), and women's threat could be divorce or some mild form of non-cooperation. Ramos shows that this violence increases men's resource shares but reduces women's productive capacity, reducing the amount of surplus available to the family and allocating a larger amount of this surplus to amount as well.

men.⁴ Take a reference bargaining solution where men choose to physically abuse their partners (15% of households in this context) and women choose divorce as their threat but do not act on it ($I_f = 0, I_m = 1$). Consider an alternative with the same specified threats, but where neither partner acts on them ($I_f = 0, I_m = 0$). This realistic reference *bargaining solution* is immune to the appeal of this alternative if women are unable to provide a transfer (monetary or in kind) to their partners that compensates men for their loss of power, conditional on the total surplus being greater in the alternative. In the setting where we observe violence, men are getting so much more of the family’s surplus that it is not possible for women to appeal successfully.

We now turn to a more careful examination of the bargaining structure, and of the bijections Δ_i for $i \in \{f, m\}$. This structure allows us to define the concept of individual rationality. After defining individual rationality, we show that there is only one *appeals-immune, individually-rational solution* θ^* to the bargaining problem $\langle \theta, \succsim_f, \succsim_m \rangle$.

2.2 Formally Defining Individual Rationality

In the first stage of this generic game, partners pick θ_i for $i \in \{f, m\}$. In the second stage, they take these threats as given and solve a LIC problem jointly. We solve this problem using backwards induction. Consider the second stage first.

The Nested Limited Commitment Collective Model

Consider the set of preferences with quasi-convex, twice differentiable, and increasing utility function representations $\succsim_i^{sm} \in \rho^{sm} \subset \rho$. Restrict attention to the class of bargaining problems of this nature: $\langle \theta, \succsim_f^{sm}, \succsim_m^{sm} \rangle$. The two partners have some cardinal utility function representations of their ordinal preferences, defined over private-equivalent consumption bundles and time allocated to labor, $U_f(x_f, l_f)$ and $U_m(x_m, l_m)$.

The central assumption in the nested model is that the partners reach a (conditionally) Pareto efficient outcome (as in Lewbel and Pendakur, 2019). The specified threats and whether they are carried out determines how far off of the best possible Pareto frontier a family’s outcome will be. If neither partner acts on their threat, then the family is on a frontier that is strictly above the frontier that obtains when one or both partners carry out their threat. See Figure 1. This is because acting on

⁴Our model is mildly more general than hers because it makes divorce endogenous, let’s women have threats as well, and is defined over the ordinal set of preferences, as opposed to the cardinal space of utility function representations. An application of this model to her study context might be fairly similar to the model she builds and estimates. Allowing women to threaten divorce would likely result in a prediction of the sharing rule that favors men slightly less than what she finds.

threats reduces the quality of the family's production and consumption technologies. Let $F(l_f, l_m|\theta)$ be the family's production function so that the total family income is $y = F(l_f, l_m|\theta)$, and let $A(x_f, x_m|\theta)$ be the family's consumption technology so that household demand functions are given by $z = A(x_f, x_m|\theta)$.

The main assumption in this nested model is that, conditional on the technologies a family has at their disposal, the partners reach an efficient allocation. The choice of threats results in a specific allocation on the Pareto frontier. Implementing threats results in a lower Pareto frontier for the family, and a specific allocation along that frontier. Families are conditionally efficient in the sense that they consume along the frontier that their family faces, and which frontier they face is a function of the partners' choices. See Figure 2 for graphic depictions of when partners choose to implement threats.

Because partners reach a Pareto efficient allocation (decisions over labor and consumption), the household's problem can be written using Chiappori's (1988) decentralized format. The family behaves as though it optimized some social welfare function, $\tilde{U}(U_f(x_f, l_f), U_m(x_m, l_m))$, which is increasing, differentiable, and concave in both of its arguments. By the second welfare theorem, the family's problem can be written in two stages: first, the family splits total resources between the two partners, then the two partners chose their private consumption demand and labor supply. Let $\eta(\theta) \in [0, 1]$ be the share of total family resources allocated to partner f , so that partner m gets share $1 - \eta(\theta)$ of the resources. Since partners make decisions over the consumption of public goods (i.e. goods that have externalities for other household members), they face Lindahl prices instead of market prices (Browning, Chiappori, and Lewbel, 2013). Let the Lindahl prices induced by the family-specific and threat-dependant consumption technology be $L(A(\theta)) \in \mathbb{R}_+^n$, such that $L(A(\theta)) \leq p$ when there are positive externalities. Note that the prices do not depend on the allocation choices, but are simply functions of the quality of the consumption technology and the goods that consumers may purchase. Define a *collective allocation problem with full commitment*, $\mathbb{B}(\theta) = \mathbb{B}(\theta_f, \theta_m, I_f, I_m)$, to be the following constrained optimization problem:

$$\begin{aligned} & \max_{\eta \in [0,1]} \tilde{U}(V_f(p, \eta y|\theta), V_m(p, (1 - \eta)y|\theta)) \text{ subject to} & (1) \\ & A(x_f, x_m|\theta) = z \text{ (Consumption Technology Constraint)} \\ & y = F(l_f, l_m|\theta) \text{ (Production Constraint)} \\ & p'z = y \text{ (Household Budget Constraint)} \\ & V_f(p, \eta y|\theta) = \max_{\substack{x_f \in \mathbb{R}_+^n, \\ l_f \in [0,24]}} U_f(x_f, l_f) \text{ s.t. } L(A(\theta))'x_f = \eta y \text{ (Her Choices)} \end{aligned}$$

$$V_m(p, (1 - \eta)y|\theta) = \underset{\substack{x_m \in \mathbb{R}_+^n, \\ l_m \in [0, 24]}}{\max} U_m(x_m, l_m) \text{ s.t. } L(A(\theta))'x_m = (1 - \eta)y \text{ (His Choices)}$$

The solution to $\mathbb{B}(\theta)$ is the set of household demand functions $z^*(p, y)$, the individuals' private consumption equivalents $x_f^*(L(A), \eta y)$ and $x_m^*(L(A(\theta)), (1 - \eta)y)$, labor supply decisions l_f^* and l_m^* , and the sharing rule $\eta^*(\theta)$. A unique solution is guaranteed to exist by the Lagrange multiplier theorem. The first order condition of (1) with respect to η gives the optimality condition for the division of resources between partners:

$$\frac{\partial \tilde{U}}{\partial V_f} \frac{\partial V_f}{\partial \eta} = - \frac{\partial \tilde{U}}{\partial V_m} \frac{\partial V_m}{\partial \eta} \quad (2)$$

This condition equates the marginal gain for the family from allocating the marginal unit of the family's resources to partner f 's control, to the marginal loss to the family that occurs because partner m is no longer in control of that portion of the family's resource.

If partners do not act on their threat, the family solves bargaining problem $\mathbb{B}(\theta_f, \theta_m, I_f = 0, I_m = 0)$, and each partner gets corresponding indirect utility from the efficient production and consumption technologies, and the resulting sharing rule, $V_f(p, \eta^*y|\theta_f, \theta_m, I_f = 0, I_m = 0)$ and $V_m(p, (1 - \eta^*)y|\theta_f, \theta_m, I_f = 0, I_m = 0)$. As such, each partner prefers to implement their threat ($I_f = 1 \succ_f I_f = 0$ and $I_m = 1 \succ_m I_m = 0$) if the corresponding utility function representations of their preferences yield higher values when they implement their threats. They solve the following optimization problem:

$$I_f^* = \underset{I_f \in \{0,1\}}{\operatorname{argmax}} [V_f(p, \eta^*y|\theta_f, \theta_m, I_f = 1, I_m), V_f(p, \eta^*y|\theta_f, \theta_m, I_f = 0, I_m)] \quad (3)$$

$$I_m^* = \underset{I_m \in \{0,1\}}{\operatorname{argmax}} [V_m(p, (1 - \eta^*)y|\theta_f, \theta_m, I_f, I_m = 1), V_m(p, (1 - \eta^*)y|\theta_f, \theta_m, I_f, I_m = 0)]$$

The *collective allocation problem with limited commitment* is $\mathbb{B}(\theta_f, \theta_m, I_f^*, I_m^*)$. The solution to this problem is, conditional on the specified threats, the indicators for whether partners act on their threats, the optimal demand and supply functions, and the optimal division of resources, conditional on the quality of the production function and consumption technology. It would be optimal to reduce the total surplus that the family has access to by acting on the specified threat if the resulting change in the sharing rule increases an individuals' total consumption. That is, the increase in their "slice of the pie" more than offsets the decrease in the "total size of the pie." Also note that for any specified pair of threats there is also a corresponding

compensating variation value that makes partners indifferent between implementing their threat and not implementing their threat. That is, there is some compensating variation value that makes partners indifferent between two different *collective allocation problems with limited commitment*.

The First Stage of the Generic Game: Choosing Threats

While Harsanyi is relatively vague about how these threats damage players, we can specify how these damages occur more clearly in the family context.

Definition 2: Let $\theta_i, \bar{\theta}_i \in (\Sigma_f \times \Sigma_m) \times \{0, 1\}^2$ be two potential threats for partner $i \in \{f, m\}$. The threat θ_i is more damaging than $\bar{\theta}_i$ if one or both of the following is true:

1. for $i \neq j \in \{f, m\}$, $F(l_f, l_m | \theta_i, \theta_j, I_i = 1, I_j) < F(l_f, l_m | \bar{\theta}_i, \theta_j, I_i = 1, I_j)$ (The more damaging threat, if carried out, lowers family income.)
2. for $i \neq j \in \{f, m\}$, $L(A(\theta_i, \theta_j, I_i = 1, I_j)) > L(A(\bar{\theta}_i, \theta_j, I_i = 1, I_j))$ (The more damaging threat, if carried out, increases the shadow prices each person faces in their optimization problems.)

Whenever someone specifies a more damaging threat, it must be because they gain additional control over the decision making process by doing so. So for any $\theta_f, \bar{\theta}_f \in \Sigma_f \times \{0, 1\}$, and for any $\theta_m \in \Sigma_m \times [0, 1]$, where θ_f is *more damaging* than $\bar{\theta}_f$, $\eta(\theta_f, \theta_m, I_f, I_m) > \eta(\bar{\theta}_f, \theta_m, I_f, I_m)$. The symmetric statement is true for partner m . If more damaging threats did not confer more control over the decision making process, the optimal threat would be the least damaging one and it would never be implemented.

Partners choose their threats from the space of possible threats to maximize their payouts in the resulting *collective allocation problem with limited commitment*. We can set up this constrained maximization problem using the cardinal utility functions, and on ordinal preferences using the bijections Δ_f and Δ_m . We first describe the cardinal problem, then formally define these bijections, then set up the corresponding ordinal problems, and finish with the definition of *individual-rationality*.

$$\theta_f^* = \underset{\theta_f \in \Sigma_f}{\operatorname{argmax}} \quad V_f(L(A(\theta_f, \theta_m, I_f^*, I_m^*), \eta^*(\theta_f, \theta_m) F(l_f^*, l_m^* | \theta_f, \theta_m, I_f^*, I_m^*))) \quad (4)$$

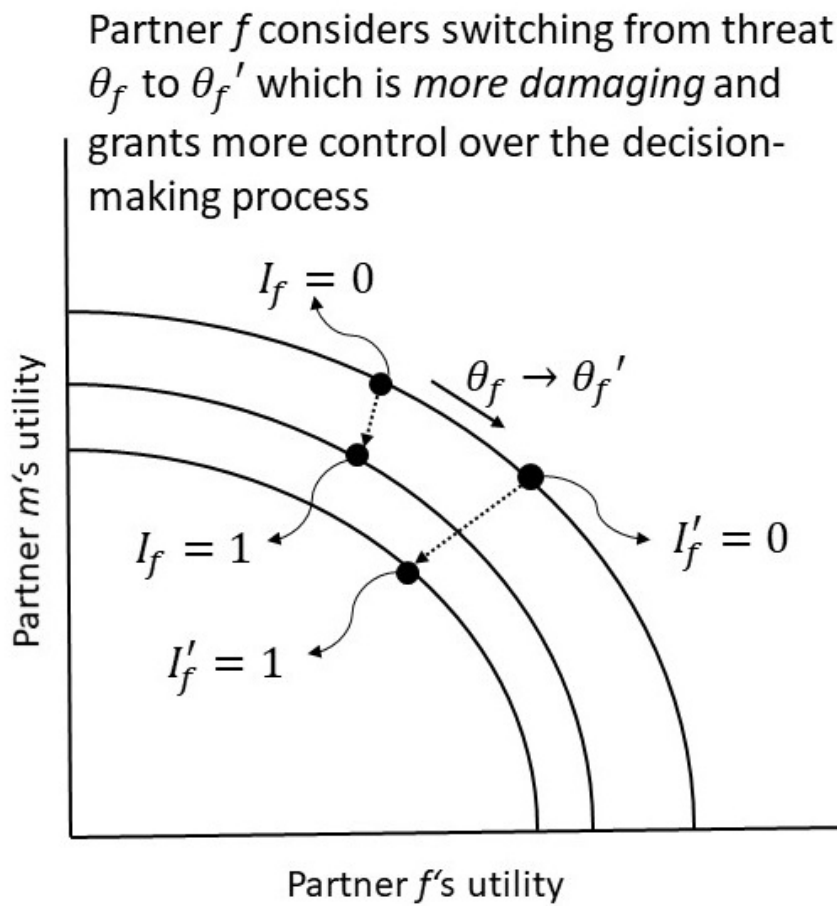


Figure 1: Partner f considers two different threats. The *more damaging* threat grants more bargaining power to partner f , shifting them along the fully efficient Pareto frontier if not implemented. If implemented, the *more damaging* threat moves the family to a lower Pareto frontier than the less damaging threat would, if it were implemented.

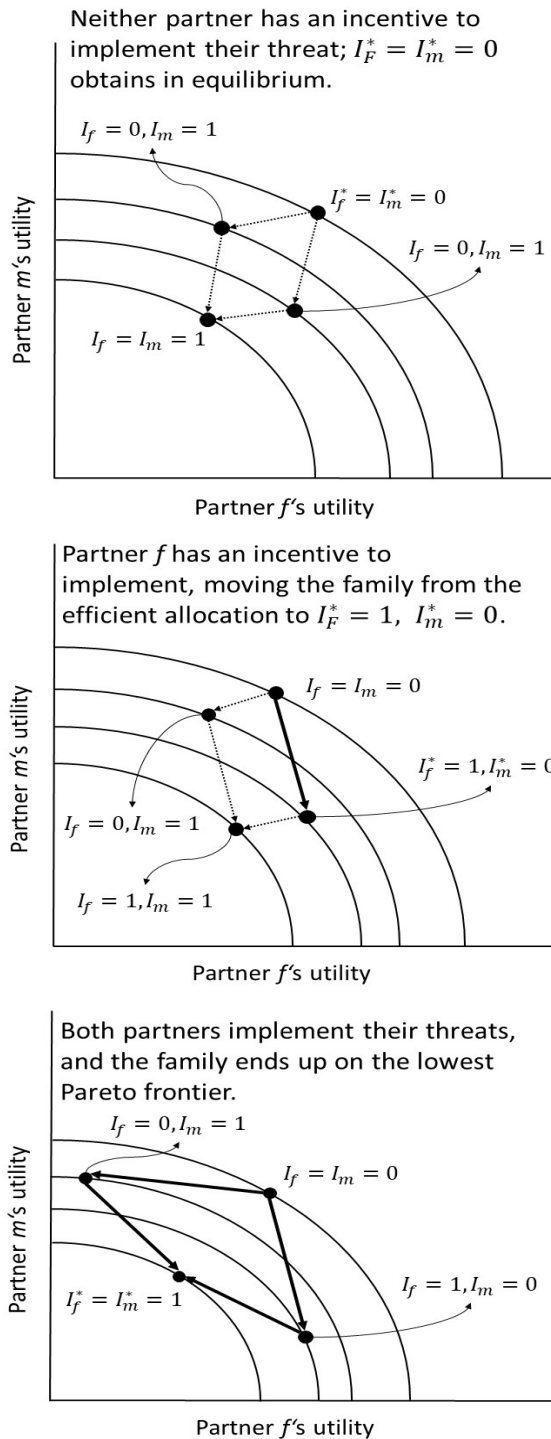


Figure 2: In the top panel, the threats that the partners have specified results in the fully-efficient equilibrium. In the middle panel, one of the partners has an incentive to implement their threat, and the family ends up on an intermediate Pareto frontier. In the bottom panel, both partners have an incentive to implement their threat and end up on the lowest Pareto frontier for their family.

$$\theta_m^* = \underset{\theta_m \in \Sigma_m}{\operatorname{argmax}} V_m(L(A(\theta_f, \theta_m, I_f^*, I_m^*), (1 - \eta^*(\theta_f, \theta_m))F(l_f^*, l_m^*|\theta_f, \theta_m, I_f^*, I_m^*)))$$

The choice of a threat influences utility in three ways. A more punishing threat moves the resource share in a person's favor, and more punishing threats damage the consumption and production technologies more. These optimization problems have the following first order conditions (suppressing notation):

$$-\frac{\frac{\partial V_f}{\partial L(A(\theta_f, \theta_m, I_f^*, I_m^*))}}{\frac{\partial L(A(\theta_f, \theta_m, I_f^*, I_m^*))}{\partial \theta_f}} = \frac{\frac{\partial V_f}{\partial \eta^*(\theta_f, \theta_m)} \frac{\partial \eta^*(\theta_f, \theta_m)}{\partial \theta_f}}{\frac{\partial V_f}{\partial F(l_f^*, l_m^*|\theta_f, \theta_m, I_f^*, I_m^*)} \frac{\partial F(l_f^*, l_m^*|\theta_f, \theta_m, I_f^*, I_m^*)}{\partial \theta_f}} \quad (5)$$

$$-\frac{\frac{\partial V_m}{\partial L(A(\theta_f, \theta_m, I_f^*, I_m^*))}}{\frac{\partial L(A(\theta_f, \theta_m, I_f^*, I_m^*))}{\partial \theta_m}} = \frac{\frac{\partial V_m}{\partial \eta^*(\theta_f, \theta_m)} \frac{\partial \eta^*(\theta_f, \theta_m)}{\partial \theta_m}}{\frac{\partial V_m}{\partial F(l_f^*, l_m^*|\theta_f, \theta_m, I_f^*, I_m^*)} \frac{\partial F(l_f^*, l_m^*|\theta_f, \theta_m, I_f^*, I_m^*)}{\partial \theta_m}} \quad (6)$$

These first order conditions in (5) equate the marginal benefit that accrues to partner f from having a larger resource share to the marginal disutility that accrues because the Pareto frontier for the family shifts inwards when the threats are acted on. Equation (6) gives the corresponding relationship for partner m .

There may be multiple pairs (θ_f^*, θ_m^*) such that (5) and (6) hold simultaneously. The threats in any such pair are *individually – rational* in $\langle \theta, \succsim_f^{sm}, \succsim_m^{sm} \rangle$. Note that any pair (θ_f^*, θ_m^*) that satisfies (5) and (6) implies that the couple solves a distinct *collective allocation problem with limited commitment* $\mathbb{B}(\theta_f^*, \theta_m^*, I_f^*, I_m^*)$. By the Kuhn-Tucker theorem, each nested game has a unique solution, including specific private consumption equivalents and labor allocations for each partner. As such, each pair is associated with a specific level of indirect utility for each partner. The differential operators relating the pair (θ_f^*, θ_m^*) to consumption and labor outcomes are:

$$\Delta_f(\theta_f^*, \theta_m^*, \succsim_f, \succsim_m, \tilde{U}) =$$

$$\left\{ (x_f^*(L(A), \eta^*y), l_f^*(L(A), \eta^*y)) \in \mathbb{R}_+^n \times [0, 24] \mid \text{conditions (2) and (5) hold} \right\}$$

$$\Delta_m(\theta_f^*, \theta_m^*, \succsim_f, \succsim_m, \tilde{U}) =$$

$$\left\{ (x_m^*(L(A), (1-\eta^*)y), l_m^*(L(A), (1-\eta^*)y)) \in \mathbb{R}_+^n \times [0, 24] \mid \text{conditions (2) and (6) hold} \right\}$$

As such, we can define preferences directly over threats for each player. By defining preferences over threats, we can define the concept of *individual-rationality* of threats without referencing the cardinal utility function representation of underlying preferences, and without needing to specify a functional form for the family's social welfare function.⁵

Definition 3: Let $\langle \theta, \succsim_f^{sm}, \succsim_m^{sm} \rangle \in (\Sigma_f \times \Sigma_m) \times (\rho^{sm})^2$ be a bargaining problem. Let $\theta^* \in (\Sigma_f \times \Sigma_m) \times [0, 1]^2$ be a potential solution. The potential solution θ is individually rational if both of the following are true:

1. $\forall \theta_m \in \Sigma_m$, and $\theta_f^* \in \Sigma_f$, $\forall \bar{\theta}_f \in \Sigma_f \setminus \{\theta_f^*\}$, $\theta_f^* \succsim_f \bar{\theta}_f \iff \Delta_f(\theta_f^*, \theta_m, \succsim_f, \succsim_m, \tilde{U}) \succsim_f \Delta_f(\bar{\theta}_f, \theta_m, \succsim_f, \succsim_m, \tilde{U})$ and
2. $\forall \theta_f \in \Sigma_f$, and $\theta_m^* \in \Sigma_m$, $\forall \bar{\theta}_m \in \Sigma_m \setminus \{\theta_m^*\}$, $\theta_m^* \succsim_m \bar{\theta}_m \iff \Delta_m(\theta_f, \theta_m^*, \succsim_f, \succsim_m, \tilde{U}) \succsim_m \Delta_m(\theta_f, \bar{\theta}_m, \succsim_f, \succsim_m, \tilde{U})$.

This definition states that people prefer a threat if they prefer the corresponding outcome from the specific resulting nested game. Let $(\Sigma_f^* \times \Sigma_m^*) \subset (\Sigma_f \times \Sigma_m)$ be the set of all potential *solutions* that are *individually-rational* for the bargaining game $\langle \theta, \succsim_f^{sm}, \succsim_m^{sm} \rangle \in (\Sigma_f \times \Sigma_m) \times (\rho^{sm})^2$.

2.3 Uniqueness of the Appeals-Immune, Individually-Rational Solution

We now turn to a discussion of existence and uniqueness of a *solution* to the bargaining problem $\langle \theta, \succsim_f, \succsim_m \rangle$. We follow Hanany and Safra (2000) to show that, for preferences satisfying certain assumptions, there is only one possible reference solution, θ^* , such that, for any possible alternative θ , θ^* is immune to the appeal of the alternative θ in $\langle \theta, \succsim_f, \succsim_m \rangle$.⁶ The following assumptions on the threat spaces, and the preferences, must hold for existence and uniqueness.

⁵In general, children's utility would enter into the social welfare function (and potentially also into parents' preferences directly), extending the model to do so does not change our results or suggested estimation strategy.

⁶The following assumptions correspond to assumptions DOM, Q, CCE, and H in Rubinstein, Safra, and Thomson (1992).

Assumption 3.3.1 — Compactness: Consider $\theta^a, \theta^b \in (\Sigma_f \times \Sigma_m)$. Consider the infinite sequence of solutions $\{\theta^a, \alpha_1\theta^a + (1-\alpha_1)\theta^b, \alpha_2\theta^a + (1-\alpha_2)\theta^b, \dots, \theta^b\} \forall \alpha_1, \alpha_2, \dots, \alpha_\infty \in [0, 1]$ such that $\alpha_1 < \alpha_2 < \dots < \alpha_\infty$. Then $\theta_a \in (\Sigma_f^* \times \Sigma_m^*) \implies \theta_b \in (\Sigma_f^* \times \Sigma_m^*)$. That is, $(\Sigma_f^* \times \Sigma_m^*)$ contains all of its limit points.

Assumption 3.3.2 — Convexity: $\forall i \in \{f, m\}, \forall \alpha \in [0, 1] \forall \theta^{*a}, \theta^{*b} \in (\Sigma_f^* \times \Sigma_m^*), \theta^{*a} \succ_i \theta^{*b} \implies \alpha\theta^{*a} + (1-\alpha)\theta^{*b} \succ_i \theta^{*b}$.

Assumption 3.3.3 — Concavity of Induced Utility Functions: Consider $\theta^a, \theta^b \in (\Sigma_f \times \Sigma_m)$, $\theta^a \succ_i \theta^b$ for $i \in \{f, m\}$, $\alpha \in (0, 1)$. The induced utility function $u(\succ_i, \theta^a, \theta^b)$ is concave if $u(\succ_i, \alpha\theta^a + (1-\alpha)\theta^b, \theta^b) > \alpha u(\succ_i, \theta^a, \theta^b) + (1-\alpha)u(\succ_i, \theta^b, \theta^b) = \alpha u(\succ_i, \theta^a, \theta^b) + 0 = \alpha u(\succ_i, \theta^a, \theta^b)$.

Assumption 3.3.4 — Loss Aversion: Preferences that have induced utilities that satisfy the following property are said to be loss-averse preferences: for $\theta^r \succ_i \theta$, $u(\succ_i, \theta, \theta^r) < |u(\succ_i, \theta^r, \theta)|$. That is, person i needs more compensation to be willing to move from a good reference to a bad alternative than they would be willing to pay to move from that bad alternative to the good reference.

Assumption 3.3.5 — Weakly Symmetric Loss Aversion (WSLA): Consider two possible solutions, $\theta, \theta^r \in (\Sigma_f \times \Sigma_m)$. When partners in a marriage have preferences that jointly exhibit the following property, they are said to be weakly symmetric in loss aversion:

1. \succ_i is loss averse for $i \in \{f, m\}$, and
2. for $\theta^r \succ_f \theta$ and $\theta \succ_m \theta^r$, $u(\succ_f, \theta^r, \theta) \leq |u(\succ_m, \theta^r, \theta)|$, and
3. for $\theta^r \succ_m \theta$ and $\theta \succ_f \theta^r$, $u(\succ_m, \theta^r, \theta) \leq |u(\succ_f, \theta^r, \theta)|$.

Let the set of preferences that satisfies assumptions 3.3.2 - 3.3.5 be denoted ρ^{WSLA} . Let the compact subset of *individually-rational solutions* be denoted $(\Sigma_f^* \times \Sigma_m^*)^C$. Formally, assumptions 3.3.4 and 3.3.5 play the same role as the bounds assumption in (E2) of Theorem 3.2 of Hanany and Safra (2000), and their risk aversion assumption. In the setting with lotteries, the risk aversion assumption is almost the exact analog of the loss aversion in the setting without uncertainty. The WSLA assumption bounds the induced utilities that result from appeals to move away from the appeals-immune *solution*, as we see in the proof of the following proposition:

Proposition - Uniqueness: Let $\langle \theta, \succ_f, \succ_m \rangle \in (\Sigma_f^* \times \Sigma_m^*)^C \times (\rho^{sm} \cap \rho^{WSLA})^2$ be a bargaining problem. Let $\theta^* \in (\Sigma_f^* \times \Sigma_m^*)^{C*} \times \{0, 1\}^2$ be a potential solution to

$\langle \theta, \succsim_f, \succsim_m \rangle$. For all possible alternatives, $\theta \in ((\Sigma_f \times \Sigma_m) \times [0, 1]^2) \setminus \{\theta^*\}$, θ^* is immune to the appeal of θ in $\langle \theta, \succsim_f, \succsim_m \rangle$ if:

$$\theta^* = \underset{\theta^* \in (\Sigma_f^* \times \Sigma_m^*)^{C^*}}{\operatorname{argmax}} \quad \prod_{i \in \{f, m\}} u(\succsim_i, \theta^*, \theta).$$

Proof. $\theta^* = \underset{\theta^* \in (\Sigma_f^* \times \Sigma_m^*)^{C^*}}{\operatorname{argmax}} \quad \prod_{i \in \{f, m\}} u(\succsim_i, \theta^*, \theta)$ is unique because $u(\succsim_i, \theta^*, \theta) \in \mathbb{R}_+$ and $u(\succsim_i, \theta^*, \theta)$ is concave. At this point,

$$\begin{aligned} \theta^* &= \underset{\theta^* \in (\Sigma_f^* \times \Sigma_m^*)^{C^*}}{\operatorname{argmax}} \quad \prod_{i \in \{f, m\}} u(\succsim_i, \theta^*, \theta) \iff \\ \frac{\partial u(\succsim_f, (\theta_f^*, \theta_m^*), (\theta_f, \theta_m))}{\partial \theta_f^*} &= - \frac{\partial u(\succsim_m, (\theta_f^*, \theta_m^*), (\theta_f, \theta_m))}{\partial \theta_f^*} \text{ and} \\ - \frac{\partial u(\succsim_f, (\theta_f^*, \theta_m^*), (\theta_f, \theta_m))}{\partial \theta_m^*} &= \frac{\partial u(\succsim_m, (\theta_f^*, \theta_m^*), (\theta_f, \theta_m))}{\partial \theta_m^*} \end{aligned}$$

These first order conditions say that at the solution, $\theta^* = (\theta_f^*, \theta_m^*)$, specifying an alternative reference results in a marginal benefit (higher willingness to pay to switch from the reference to the alternative) to one partner equal to the marginal cost (higher willingness to pay to avoid switching from the reference to the alternative) to the other player. We can move away from the equilibrium in one of four directions of interest, corresponding to the two conditions in Definition 1. When we move away from the equilibrium, the equalities in the first order conditions hold as inequalities. Because preferences satisfy WSLA, we know which direction the inequality will go in for each case. To formalize the idea of "moving away from the equilibrium," consider also some convex mixture of θ^* and θ . These four conditions are, for some small $\alpha \in (0, 1)$:

1. Partner f prefers the change in partner f 's threat, and partner m does not: $(\alpha\theta_f^* + (1-\alpha)\theta_f, \theta_m^*) \succ_f (\theta_f^*, \theta_m^*)$ and $(\theta_f^*, \theta_m^*) \succ_m ((\alpha\theta_f^* + (1-\alpha)\theta_f), \theta_m^*)$. If this is true, and because preferences satisfy the WSLA assumption, the FOCs imply $u(\succsim_f, (\alpha\theta_f^* + (1-\alpha)\theta_f), \theta_m^*), (\theta_f^*, \theta_m^*) < |u(\succsim_m, (\alpha\theta_f^* + (1-\alpha)\theta_f), \theta_m^*), (\theta_f^*, \theta_m^*)|$ and so no transfer, τ_f , exists such that $(\alpha\theta_f^* + (1-\alpha)\theta_f), \theta_m^*)$ successfully appeals θ^* .
2. Partner f prefers the change in partner m 's threat, and partner m does not: $(\theta_f^*, (\alpha\theta_m^* + (1-\alpha)\theta_m)) \succ_f (\theta_f^*, \theta_m^*)$ and $(\theta_f^*, \theta_m^*) \succ_m (\theta_f^*, (\alpha\theta_m^* + (1-\alpha)\theta_m))$. If this is true, and because preferences satisfy the WSLA assumption, then the FOCs imply $u(\succsim_f, (\theta_f^*, (\alpha\theta_m^* + (1-\alpha)\theta_m)), (\theta_f^*, \theta_m^*) < |u(\succsim_m, (\theta_f^*, (\alpha\theta_m^* + (1-\alpha)\theta_m)), (\theta_f^*, \theta_m^*)|$

$\alpha)\theta_m), \theta_m^*), (\theta_f^*, \theta_m^*))$ and so no transfer, τ_f , exists such that $(\theta_f^*, (\alpha\theta_m^* + (1 - \alpha)\theta_m))$ successfully appeals θ^* .

3. Partner m prefers the change in partner f 's threat, and partner f does not: $((\alpha\theta_f^* + (1 - \alpha)\theta_f), \theta_m^*) \succ_m (\theta_f^*, \theta_m^*)$ and $(\theta_f^*, \theta_m^*) \succ_f ((\alpha\theta_f^* + (1 - \alpha)\theta_f), \theta_m^*)$. If this is true, and because preferences satisfy the WSLA assumption, then the FOCs imply $|u(\succ_f, (\alpha\theta_f^* + (1 - \alpha)\theta_f), \theta_m^*), (\theta_f^*, \theta_m^*)| > u(\succ_m, (\alpha\theta_f^* + (1 - \alpha)\theta_f), \theta_m^*), (\theta_f^*, \theta_m^*))$ and so no transfer, τ_m , exists such that $(\alpha\theta_f^* + (1 - \alpha)\theta_f), \theta_m^*)$ successfully appeals θ^* .
4. Partner m prefers the change in partner m 's threat, and partner f does not: $(\theta_f^*, (\alpha\theta_m^* + (1 - \alpha)\theta_m)) \succ_m (\theta_f^*, \theta_m^*)$ and $(\theta_f^*, \theta_m^*) \succ_f (\theta_f^*, (\alpha\theta_m^* + (1 - \alpha)\theta_m))$. If this is true, and because preferences satisfy the WSLA assumption, then the FOCs imply $|u(\succ_f, (\theta_f^*, (\alpha\theta_m^* + (1 - \alpha)\theta_m)), (\theta_f^*, \theta_m^*))| > u(\succ_m, (\theta_f^*, (\alpha\theta_m^* + (1 - \alpha)\theta_m)), \theta_m^*), (\theta_f^*, \theta_m^*))$ and so no transfer, τ_m , exists such that $(\theta_f^*, (\alpha\theta_m^* + (1 - \alpha)\theta_m))$ successfully appeals θ^* .

Because $(\Sigma_f^* \times \Sigma_m^*)^C$ is compact, and because the above argument holds for any possible reference, the θ^* that maximizes the Nash product of induced utilities over WSLA preferences is the unique *appeals-immune solution* to the *bargaining problem* $\langle \theta, \succ_f, \succ_m \rangle \in (\Sigma_f^* \times \Sigma_m^*)^C \times (\rho^{WSLA})^2$. ■

This model with endogenous threats and resource shares allows us to understand power dynamics in the family more fully. Who ever is capable of specifying a more damaging threat will have more control over the household decision making process. Compared to the standard collective model, this generic game with a nested limited commitment problem allows us to understand why we observe certain sharing rules for each family. It allows us to measure power dynamics without assuming that only one partner can specify or act on a threat that reduces household efficiency.

3 Identification

In this section, we lay out two possible semi-parametric identification strategies that have different data requirements, and give a brief synopsis of when one might be preferable to the other. We begin with a strategy that treats preferences as random variables, allowing us to avoid specific functional form assumptions for many of the functions introduced in section 3.2. Using this approach, the researcher recovers the expected value of the sharing rule. Then, we give a semi-parametric identification strategy that is similar to the one in Browning, Chiappori, and Lewbel (2013). In this approach, functional form assumptions cannot be avoided. However, the researcher

recovers a functional form for the sharing rule itself, instead of the expected value of the sharing rule.

In both cases, the first step in estimating the model is to quantify how damaging each threat is. This can be accomplished by using violence scales, like the one Ramos (2016) uses. This approach generates a scale from 0 to 1 that describes the severity of the threat. Each possibility is given some (normalized) value, and the score is the sum of the quantified individual actions comprising a threat. For instance, a women who is punched and verbally threatened with a weapon would have a higher score than a woman who is only threatened with a weapon. A women who is only punched would have a higher score than a woman who is only threatened.

In order to incorporate all types of threats into our model, we must also assign values to actions like divorce and the inefficient allocation of productive assets. This is a necessarily subjective exercise, but is based on the objective change in real incomes that each partner would have if the threat is exercised. Ideally, the threat scale would assign higher values to threats that reduce the real income available to an individual's partner by a greater amount. Since divorce (and any threat that ends cohabitation) results in both partners consuming at market prices, and consuming according to their own private incomes instead of a shared income, divorce can be given a higher scale value than violence. We suggest that any threat which only reduces the quality of the production function be given the lowest values in the scale, any threat that only reduces the quality of the consumption technology be given the next highest values, and any threat that affects both be given higher values. Various scales could be used to test the robustness of the results to various scale specifications.

3.1 An Identification Strategy Over Ordinal Preferences

Summary of requirements: The researcher must have access to panel data with at least two waves for each household. Each wave must have demographic information about each partner (for instance their age, earnings, and education), and information about the threats that partners might specify (for instance, domestic abuse or divorce). From this information, we can learn the threats partners specify, and whether they implement them. The values that we will estimate are the threats for partners who do not act on them, the real incomes for each household in the context we do not observe (for instance, in the case where $I_f = 0$ when we observe $I_f = 1$), and the expected value of the sharing rule. The assumptions required are distributional assumptions on preferences, distributional assumptions on the sharing rule in the cases we do not observe, and $H + 2$ distributional assumptions on regression coefficients to be estimated using the simulated method of moments (McFadden,

1989), where H is the number of households in the sample. These assumptions on the coefficient distributions are analogous to a single assumption on the distribution of the error term in a fixed effects model with H constraints on the intercepts, estimated using constrained least squares.

An optional, but helpful, data feature is an instrument that is correlated with how damaging each partners' threat is, and uncorrelated with whether or not they implement their threat. Lewbel and Pendakur (2019) use the thickness of each person's walls (a proxy for how likely it is that partners overhear domestic abuse) as an instrument in a similar setting. For instance, if you're worried about being overheard, you might specify a threat that does not entail loud volumes. If so, implementing the threat is uncorrelated with the likelihood of being overheard. Access to such an instrument makes estimation arguably less biased.

Strategy: First, note that the optimization problems in (3.3) can be rewritten without reference to the indirect utility functions by applying a compensating variation approach within the nested game with limited commitment, $B(\theta_f, \theta_m, I_f^*, I_m^*)$. For any threat, there is some transfer value that makes partners indifferent between the prices they face in the collective allocation ($I_i = 0$) and the inefficient allocation ($I_i = 1$) for $i \in \{f, m\}$. These transfer amounts make the partners indifferent between the price settings they face in both settings, but the real income they would have at their disposal may still differ across the two collective and less efficient equilibria. Denote these transfer amounts γ_f and γ_m , such that

$$V_f(L(A(\theta_f, \theta_m, I_f = 1, I_m)), \eta y) = V_f(L(A(\theta_f, \theta_m, I_f = 0, I_m)), \eta y + \gamma_f) \text{ and}$$

$$V_m(L(A(\theta_f, \theta_m, I_f, I_m = 1)), (1 - \eta)y) = V_m(L(A(\theta_f, \theta_m, I_f, I_m = 0)), (1 - \eta)y + \gamma_m).$$

By holding prices constant across the indirect utility functions, only the second argument in the function varies with different threats. The impact on shadow incomes is captured by the changes in the sharing rule and the production function, and the impact on the price setting is captured by the compensating variation amount. The indirect utility functions are strictly increasing in their second argument. As such, the problems in (3) can be re-written in a form that does not explicitly reference the indirect utility function. In this formulation, the individuals consider the real (shadow) income they would have at their disposal in the collective and inefficient allocations and chooses to implement their threat if doing so gives a greater real income. That is, the partners solve the following, equivalent problems, where both options are measured in dollar amounts:

$$\max_{I_f \in \{0,1\}} \left(\eta(\theta_f, \theta_m, I_f = 1, I_m) F(\theta_f, \theta_m, I_f = 1, I_m), \right. \\ \left. \eta(\theta_f, \theta_m, I_f = 0, I_m) F(\theta_f, \theta_m, I_f = 0, I_m) + \gamma_f \right)$$

$$\max_{I_m \in \{0,1\}} \left((1 - \eta(\theta_f, \theta_m, I_f, I_m = 1)) F(\theta_f, \theta_m, I_f, I_m = 1), \right. \\ \left. (1 - \eta(\theta_f, \theta_m, I_f, I_m = 0)) F(\theta_f, \theta_m, I_f, I_m = 0) + \gamma_m \right)$$

We observe I_f^* and I_m^* , so we know which of the two options has a higher value. There are four possibilities: the fully efficient outcome ($I_f = 0, I_m = 0$), he implements his threat but she does not ($I_f = 0, I_m = 1$), she implements her threat but he does not ($I_f = 1, I_m = 0$), and both implement their threats ($I_f = 1, I_m = 1$). In each case, we get family-specific bounds on the possible values that the sharing rule can take. These bounds, when paired with a joint distributional assumption on the partners' preferences, result in a functional form for the expected value of the sharing rule that we can bring to data.

We derive the bounds next, then describe the remaining estimation steps: (1) assuming a distribution on preferences, (2) using a Heckman (1979) selection approach to recover estimates of threats for those who do not implement threats, (3) using a propensity score matching approach to recover the real (shadow) incomes in the unobserved cases, and (4) recovering the remaining parameters that determine the family-specific bounds on the sharing rule by estimating a fixed effects model using the simulated method of moments. To make equations more legible, let $\theta^e = (\theta_f, \theta_m, I_f = 0, I_m = 0)$, $\theta^{her} = (\theta_f, \theta_m, I_f = 1, I_m = 0)$, $\theta^{him} = (\theta_f, \theta_m, I_f = 0, I_m = 1)$, and $\theta^{both} = (\theta_f, \theta_m, I_f = 1, I_m = 1)$.

Case 1: The Fully Efficient Outcome: Because we observe ($I_f = 0, I_m = 0$), we know that

$$\eta(\theta^e) F(\theta^e) + \gamma_f > \eta(\theta^{her}) F(\theta^{her}) \text{ and} \\ (1 - \eta(\theta^e)) F(\theta^e) + \gamma_m > (1 - \eta(\theta^{him})) F(\theta^{him}).$$

Solving these two inequalities for $\eta(\theta^e)$, the sharing rule that results in equilibrium,

gives the following bounds:

$$\eta(\theta^e) \in \left[\frac{\eta(\theta^{her})F(\theta^{her}) - \gamma_f}{F(\theta^e)}, 1 - \frac{(1 - \eta(\theta^{him}))F(\theta^{him}) - \gamma_m}{F(\theta^e)} \right].$$

Here, we observe $F(\theta^e)$ and will estimate values for θ^{her} and θ^{him} using a Heckman (1979) selection approach, and for $F(\theta^{her})$ and $F(\theta^{him})$ using a propensity score matching approach. We will recover estimates of $\eta(\theta^{her})$, $\eta(\theta^{him})$, γ_f , and γ_m from a simulated method of moments approach. These estimates and observed values pin down the family specific bounds on the possible values of the sharing rule.

Case 2: Only Partner f Implements Their Threat: Because we observe ($I_f = 1, I_m = 0$), we know that

$$\begin{aligned} \eta(\theta^e)F(\theta^e) + \gamma_f &< \eta(\theta^{her})F(\theta^{her}) \text{ and} \\ (1 - \eta(\theta^{her}))F(\theta^{her}) + \gamma_m &> (1 - \eta(\theta^{both}))F(\theta^{both}). \end{aligned}$$

Solving these two inequalities for $\eta(\theta^{her})$, the sharing rule that results in equilibrium, gives the following bounds:

$$\eta(\theta^{her}) \in \left[\frac{\eta(\theta^e)F(\theta^e) + \gamma_f}{F(\theta^{her})}, 1 - \frac{(1 - \eta(\theta^{both}))F(\theta^{both}) - \gamma_m}{F(\theta^{her})} \right].$$

Here, we observe $F(\theta^{her})$ and will estimate values for θ^e and θ^{both} using a Heckman (1979) selection approach, and for $F(\theta^e)$ and $F(\theta^{both})$ using a propensity score matching approach. We will recover estimates of $\eta(\theta^e)$, $\eta(\theta^{both})$, and $\gamma \equiv \gamma_m - \gamma_f$ from a simulated method of moments approach (which we will explain next). These estimates and observed values pin down the family specific bounds on the possible values of the sharing rule.

Case 3: Only Partner m Implements Their Threat: Because we observe ($I_f = 0, I_m = 1$), we know that

$$\begin{aligned} \eta(\theta^{him})F(\theta^{him}) + \gamma_f &> \eta(\theta^{both})F(\theta^{both}) \text{ and} \\ (1 - \eta(\theta^e))F(\theta^e) + \gamma_m &< (1 - \eta(\theta^{him}))F(\theta^{him}). \end{aligned}$$

Solving these two inequalities for $\eta(\theta^{him})$, the sharing rule that results in equilibrium, gives the following bounds:

$$\eta(\theta^{him}) \in \left[\frac{\eta(\theta^{both})F(\theta^{both}) - \gamma_f}{F(\theta^{him})}, 1 - \frac{(1 - \eta(\theta^e))F(\theta^e) + \gamma_m}{F(\theta^{him})} \right].$$

Here, we observe $F(\theta^{him})$ and will estimate values for θ^e and θ^{both} using a Heckman (1979) selection approach, and for $F(\theta^e)$ and $F(\theta^{both})$ using a propensity score matching approach. We will recover estimates of $\eta(\theta^e)$, $\eta(\theta^{both})$, and $\gamma \equiv \gamma_m - \gamma_f$ from a simulated method of moments approach. These estimates and observed values pin down the family specific bounds on the possible values of the sharing rule.

Case 4: Both Partners Implement Their Threats: Because we observe $(I_f = 1, I_m = 1)$, we know that

$$\eta(\theta^{him})F(\theta^{him}) + \gamma_f < \eta(\theta^{both})F(\theta^{both}) \text{ and}$$

$$(1 - \eta(\theta^{her}))F(\theta^{her}) + \gamma_m < (1 - \eta(\theta^{both}))F(\theta^{both}).$$

Solving these two inequalities for $\eta(\theta^{both})$, the sharing rule that results in equilibrium, gives the following bounds:

$$\eta(\theta^{both}) \in \left[\frac{\eta(\theta^{him})F(\theta^{him}) + \gamma_f}{F(\theta^{both})}, 1 - \frac{(1 - \eta(\theta^{her}))F(\theta^{her}) + \gamma_m}{F(\theta^{both})} \right].$$

Here, we observe $F(\theta^{him})$ and will estimate values for θ^e and θ^{both} using a Heckman (1979) selection approach, and for $F(\theta^e)$ and $F(\theta^{both})$ using a propensity score matching approach. We will recover estimates of $\eta(\theta^e)$, $\eta(\theta^{both})$, and $\gamma \equiv \gamma_m - \gamma_f$ from a simulated method of moments approach. These estimates and observed values pin down the family specific bounds on the possible values of the sharing rule.

Distributional Assumptions on Preferences: At this point, we must make some assumption on preferences. Assuming that a specific functional form for utility functions adequately captures the preferences for all individuals in the sample is a strong, parametric assumption. We can make a weaker, semi-parametric assumption: that preferences and the social welfare function are random variables drawn from some joint probability distribution function from $(\rho^{sm})^2 \times S$, where S is the set of permissible social welfare functions. Doing so implies a particular distribution of the sharing rule on the set determined by the observed values (I_f, I_m) . This is because a (linear) bijection relates the specified threats, the pair (I_f, I_m) , and the drawn random variables (U_f, U_m, \tilde{U}) .⁷

A particularly tractable and weak distributional assumption is that preferences are conditionally uniformly distributed on some subset of $(\rho^{sm})^2 \times S$. Consider an arbitrarily drawn partition of $(\rho^{sm})^2 \times S$, with $c \in \mathbb{N}$ subsets $C \subset (\rho^{sm})^2 \times S$, where $\bigcup_{i \in [1, c]} C_i = (\rho^{sm})^2 \times S$. For each family in the population, let the triple (U_f, U_m, \tilde{U}) be

⁷For proofs that this bijective function exists and is linear, see Klein and Barham (2018).

uniformly drawn from the same subset, C_i . This is a very weak “similarity between partners” assumption since the partition can be drawn in any way (any number of subsets, with subsets of any size). This distributional assumption on preferences results in a uniform distribution of the sharing rule on the family-specific bounds derived above. As such, the estimator of the sharing rule can be written as follows in each of the four cases:

1. $\mathbb{E}[\eta(\theta^e)|(U_f, U_m, \tilde{U}) \stackrel{\text{Unif}}{\sim} C_i] = \frac{1}{2} + \frac{1}{2} \left(\frac{\eta(\theta^{her})F(\theta^{her}) - (1 - \eta(\theta^{him}))F(\theta^{him}) - \gamma_f + \gamma_m}{F(\theta^e)} \right)$
2. $\mathbb{E}[\eta(\theta^{her})|(U_f, U_m, \tilde{U}) \stackrel{\text{Unif}}{\sim} C_i] = \frac{1}{2} + \frac{1}{2} \left(\frac{\eta(\theta^e)F(\theta^e) - (1 - \eta(\theta^{both}))F(\theta^{both}) + \gamma_f + \gamma_m}{F(\theta^{her})} \right)$
3. $\mathbb{E}[\eta(\theta^{him})|(U_f, U_m, \tilde{U}) \stackrel{\text{Unif}}{\sim} C_i] = \frac{1}{2} + \frac{1}{2} \left(\frac{\eta(\theta^{both})F(\theta^{both}) - (1 - \eta(\theta^e))F(\theta^e) - \gamma_f - \gamma_m}{F(\theta^{him})} \right)$
4. $\mathbb{E}[\eta(\theta^{both})|(U_f, U_m, \tilde{U}) \stackrel{\text{Unif}}{\sim} C_i] = \frac{1}{2} + \frac{1}{2} \left(\frac{\eta(\theta^{him})F(\theta^{him}) - (1 - \eta(\theta^{her}))F(\theta^{her}) + \gamma_f - \gamma_m}{F(\theta^{both})} \right)$

Estimation Process: First, we will recover the expected values of the threats that are not implemented using a Heckman (1979) selection approach. This allows us to recover estimates of these threats based on observable demographic characteristics, and an unobservable selection parameter, which describes the differences in specified threats between those who choose to implement them, and those who do not implement them. Disaggregating the sample by gender allows the econometrician to recover regression coefficients and selection parameters that differ across men and women. As such, estimate the following two models using full information maximum likelihood:

$$I_{f,h,t} = X_{f,h,t}\beta_{f,h,t} + z_{f,h,t}\beta_{instrument,f,h,t} + \epsilon_{f,h,t} \quad (7)$$

$$\theta_{f,h,t} = X_{f,h,t}\beta_{f,h,t} + \epsilon_{f,h,t}$$

$$I_{m,h,t} = X_{m,h,t}\beta_{m,h,t} + z_{m,h,t}\beta_{instrument,m,h,t} + \epsilon_{m,h,t} \quad (8)$$

$$\theta_{m,h,t} = X_{m,h,t}\beta_{m,h,t} + \epsilon_{m,h,t}$$

where t indexes time, h indexes the household that partners f and m belong to at the start of the panel, $z_{f,h,t}$ is an instrument for I_f (that is $cov(I_{f,h,t}, z_{f,h,t}) \neq 0$ and $cov(\theta_{f,h,t}, z_{f,h,t}) = 0$), $z_{m,h,t}$ is an instrument for I_m (that is $cov(I_{m,h,t}, z_{m,h,t}) \neq 0$ and $cov(\theta_{m,h,t}, z_{m,h,t}) = 0$), $X_{f,h,t}$ is a matrix of demographic characteristics for the women in the sample, and $X_{m,h,t}$ is a matrix of demographic characteristics for the men in the sample.⁸ The results are the (nuisance) regression coefficients that relate observable characteristics to the severity of the specified threat, and the likelihood

⁸The model does not require instruments, but in that case it does require an additional joint normality assumption.

that the threat is carried out, plus the (nuisance) selection coefficient estimates that describe how much threats differ on average between those who implement them and those who do not. The predictions for threats of those who do not implement them are the fitted values from these Heckman (1979) selection models: $\hat{\theta}_{f,h,t}$ and $\hat{\theta}_{m,h,t}$. We use the fitted values for all individuals for consistency.

Second, we must recover the shadow incomes for individuals in each case. We can use the predicted threats as propensity scores in a propensity score matching approach (Rosenbaum and Ruben, 1983). In each case, the econometrician needs to recover unobserved income values. We suggest using a nearest neighbor matching approach to recovering these parameters. For instance, if we observe $(I_f = 0, I_m = 0)$ for some household, then we need to recover values for $F(\theta^{him})$ and $F(\theta^{her})$. We suggest using the income value for the nearest household (nearest in the value of $\hat{\theta}_{f,h,t}$) such that that neighboring household has observed value $I_f = 1$ for the estimate of $F(\theta^{her})$. Symmetrically, we suggest using the income value for the closest neighbor in the value of $\hat{\theta}_{f,h,t}$ (where that neighbor has observed value $I_m = 1$) to recover the estimate of $F(\theta^{him})$. Denote these propensity score matching estimates as $\hat{F}(\hat{\theta}^{him})$ and $\hat{F}(\hat{\theta}^{her})$.

At this point, the remaining unknown parameter values in the bounds are the sharing rule values in the unobserved cases, and the compensating variation values, γ_f and γ_m . In order to recover these values, we suggest a fixed effects strategy. Since the approach is the same across all four cases, we only describe it for the fully efficient case. The first step in this panel estimation is to notice that the functional form for the expected value of the equilibrium sharing rule can be rearranged so that income is a linear function of the estimated shadow incomes in the unobserved cases, and unknown parameters. In the fully efficient case, this gives the following expression, suppressing notation:

$$F(\theta^e) = \frac{\eta(\theta^{her})F(\theta^{her}) - (1 - \eta(\theta^{him}))F(\theta^{him}) - \gamma_f + \gamma_m}{\mathbb{E}[\eta(\theta^e)] - 1}$$

We can estimate this equation using a fixed effects approach, with the following definitions for regression coefficients:

$$F(\theta^e)_{h,t} = \beta_{0,h} + \beta_1 \hat{F}(\hat{\theta}^{her})_{h,t} + \beta_2 \hat{F}(\hat{\theta}^{him})_{h,t} + \epsilon_{h,t} \text{ such that} \quad (9)$$

$$\beta_{0,h} \equiv \frac{\gamma_m - \gamma_f}{\mathbb{E}[\eta(\theta^e)] - 1}$$

$$\beta_1 \equiv \frac{\eta(\theta^{her})}{\mathbb{E}[\eta(\theta^e)] - 1}$$

$$\beta_2 + \epsilon_{h,t,2} \equiv \frac{1 - \eta(\theta^{him})}{\mathbb{E}[\eta(\theta^e)] - 1}$$

$$\epsilon_{h,t,2} \equiv \epsilon_{h,t} \hat{F}(\hat{\theta}^{him})$$

$$\eta^e \in [0, 1], \quad \eta^{her} \in [0, 1], \quad \text{and } \eta^{him} \in [0, 1].$$

Estimating (9) using the simulated method of moments requires the following assumptions: distributional assumptions for the H intercept parameters, $\beta_{0,h}$; distributional assumptions for the two slope parameters, β_1 and β_2 ; and distributional assumptions for the off-equilibrium sharing rule values, $\eta(\theta^{her})$ and $\eta(\theta^{him})$. Under these assumptions, there are two remaining unknowns per household in (9), and at least two equations per household in the panel. After the simulated method of moments estimation, the estimates of the regression coefficients can be plugged into the definitions in (9) to recover the expected value of the sharing rule in the equilibrium, and the difference between the two partners' compensating variation values, $\gamma_m - \gamma_f$. The constraints that the sharing rules only take values between 0 and 1 limit the regression coefficients' supports.

We suggest the following procedure for selection assumptions for the regression coefficients. First fit the regression in (9) without taking into account the adding up constraints ($\eta^e \in [0, 1]$, $\eta^{her} \in [0, 1]$, and $\eta^{him} \in [0, 1]$). This gives naive regression coefficients. Assume that the simulated method of moments coefficients for (9) are truncated normal distributions with means given by the naive estimators, and variance given by the corresponding naive standard errors. For the off-equilibrium sharing rule values, we recommend assuming uniform distributions on the unit interval. With a large number of simulations, this process will give consistent estimators of the equilibrium sharing rule and the compensating variation value difference.

3.2 An Identification Strategy Over Cardinal Representations of Ordinal Preferences

An alternative approach to identification is to assume specific functional forms for utility, the social welfare function, the consumption and production technologies, and the sharing rule, and then solving the model using backwards induction. This approach is similar to the identification strategy pursued in Browning, Chiappori, and Lewbel (2013). They assume a linear Barten-Gorman style consumption technology, PIGLOG utility functions, a Bergson-Samuelson social welfare function, and a Logit form for the sharing rule. We suggest also assuming a Cobb-Douglas production function. The resulting system of first order conditions (i.e. the equilibrium demand functions, labor supply functions, threat selection functions, and implementation choices) can be fit using the generalized method of moments (Hansen, 2001). This is an algebraically challenging but econometrically simple approach. In comparison, the ordinal approach is algebraically simple and econometrically complex.

3.3 Comparing The Two Strategies

The ordinal identification strategy is a closer empirical approach to estimating the ordinal model presented in Section 2. Using this strategy, the economist can avoid making strong functional form assumptions on utility and social welfare functions, and consumption and production technologies. This is valuable because these assumptions are unverifiable. However, the economist only recovers the expected value of the sharing rule, not an explicit formula for the sharing rule, using the ordinal approach. In addition, this approach requires panel data.

Researchers who wish to analyze the relationships between divorce, violence, the sharing rule and consumption or production decisions may prefer to use the cardinal identification strategy. For instance, researchers who want to study the effects of legislation aimed at reducing intimate partner violence on investments in children, and want to decompose the total program effects into a power effect and (real) income effects, may prefer to use the cardinal identification strategy.

4 Conclusion

It is well known that policy makers can influence intra-household bargaining power by increasing the value of one partners' outside option (Mazzocco, 2007; Voena, 2015). In the standard limited commitment model, when policies change the value of the outside option so much that one partner newly prefers to leave the marriage, bargaining power in the family is renegotiated until that partner is indifferent between leaving and staying. Only drastic changes to the outside option result in a change in bargaining power, since most changes will be insufficient to make either partner prefer divorce to the current marriage contract. As such, power is expected to be fairly static, and changes in power dynamics are often expected to be small (see, e.g., Lise and Yamada, 2019).

When partners can specify outside options besides divorce, changes in power can be fairly frequent. Partners might subtly shift their specified threat, resulting in a different sharing rule, in response to smaller changes to relative outside options. Changes that would not cause the participation constraint to bind if the outside option is divorce might cause it to bind if the outside option is changing the amount of time allocated to labor (as in Walther, 2018) or the savings technology used (as in Schaner, 2015).

A different picture of power in the family emerges. Policy makers can hope to influence power dynamics even with "small" changes to the relative value of outside options. Events like minor salary increases, or even holiday bonuses, can change the balance of power in the family. Power, once collective models make outside options

endogenous, appears to be highly variable and contested, not static.

Can policy makers influence partners' choices to specify certain threats, or pass policies that cause individuals to choose to not implement their threats? Any policy that expands individuals' space of possible threats to include more attractive possible outside options will accomplish the former. Any policy that changes the costs and benefits of implementing may achieve the latter. For instance, higher ratios of female-to-male police officers in the United States increases the likelihood that women report domestic abuse, increasing the cost of implementing that threat for men, and reducing the likelihood that they implement their threat (Miller and Segal, 2019). Our model predicts that such a policy would increase women's bargaining power, since men only implement if they gain control over the decision-making process by doing so.

In general, we would expect families to be more efficient in settings where men and women have more equal rights and opportunities. Any policy that increases equality in institutions outside of the family — like labor markets or divorce courts — gives the less powerful partner additional recourse against more damaging threats. This changes the threats that obtain in equilibrium, and shifts the bargaining power dynamic towards equality within the family.

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